

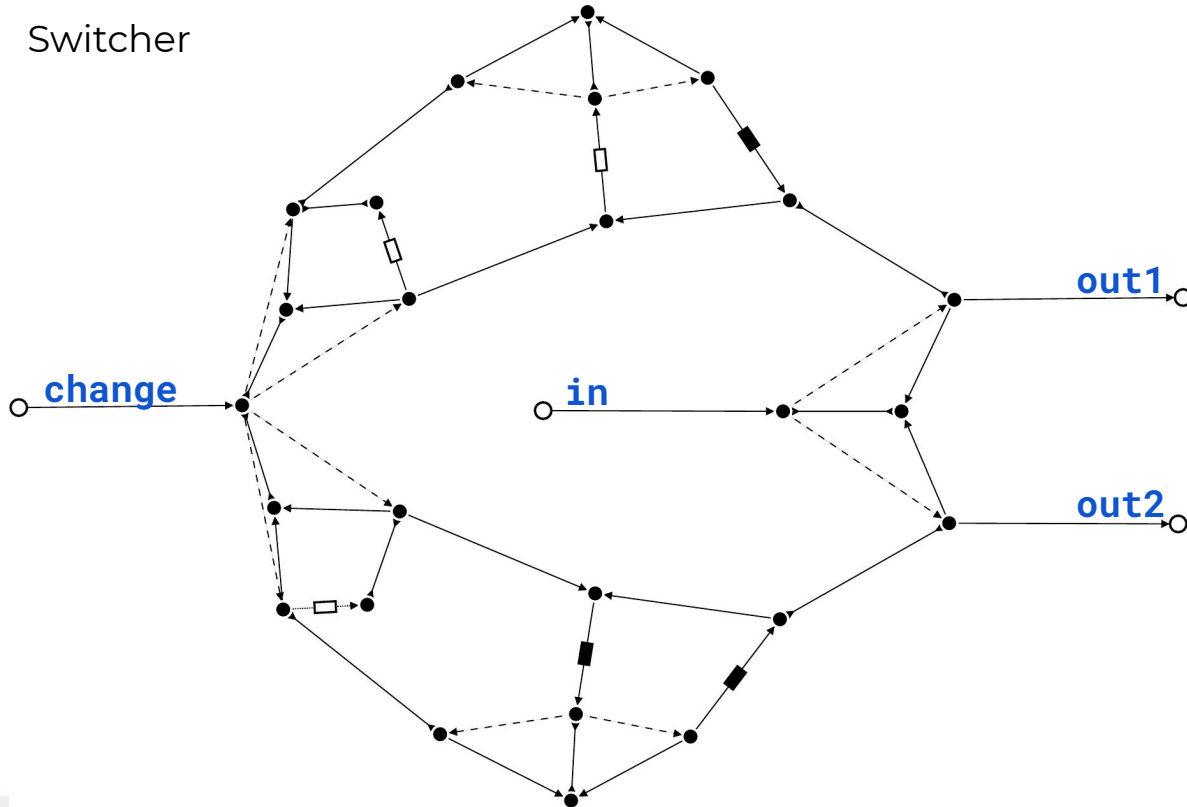
Taiming Hierarchical Connectors

José Proença & Alexandre Madeira



Universidade do Minho

Motivation

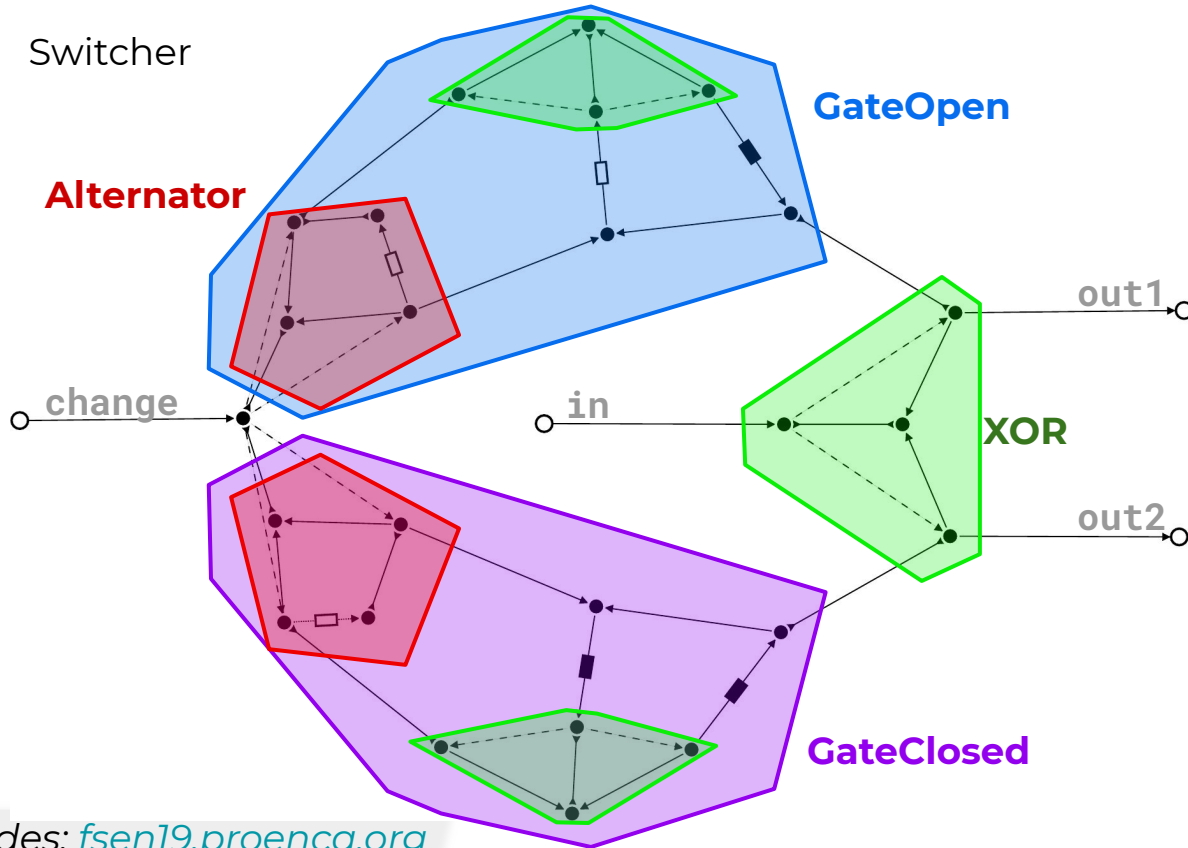


How to:

- Build
- **Verify**
behaviour

Look *inside* the
connector

Motivation

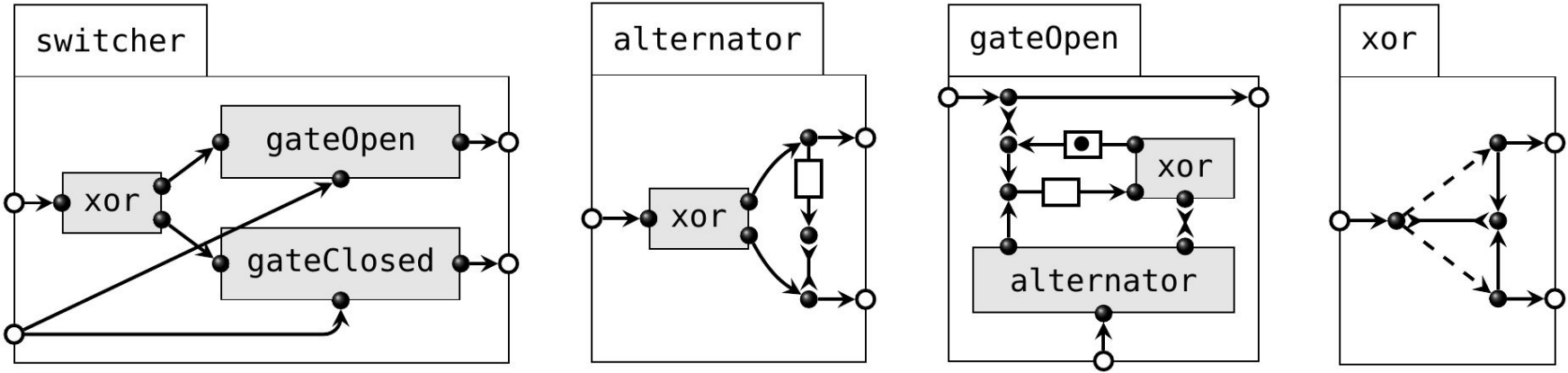


How to:

- Build
- **Verify behaviour**

Look *inside* the connector

Reason over nested containers



Containers: { switcher, alternator, gateOpen, xor, \dashrightarrow , \square , \longrightarrow , ... }

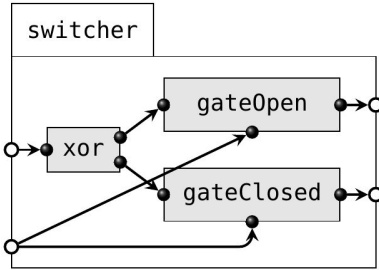
Specify and verify properties
over containers

Modal logic

M_CR_L2
analysing system behaviour

Outline

Hierarchical connectors



Logic over containers

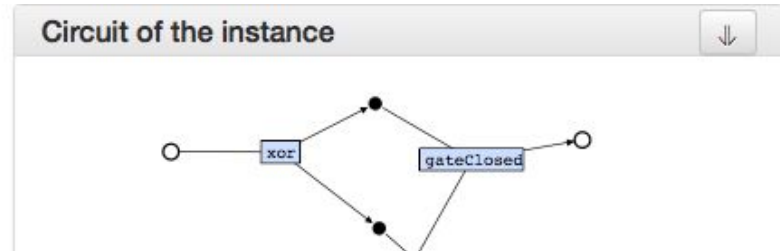
$\langle \text{all}^* . \text{gateOpen} \rangle$

$\text{@}_{\text{gateOpen}} \langle \overline{\text{alternator}}^* \rangle$

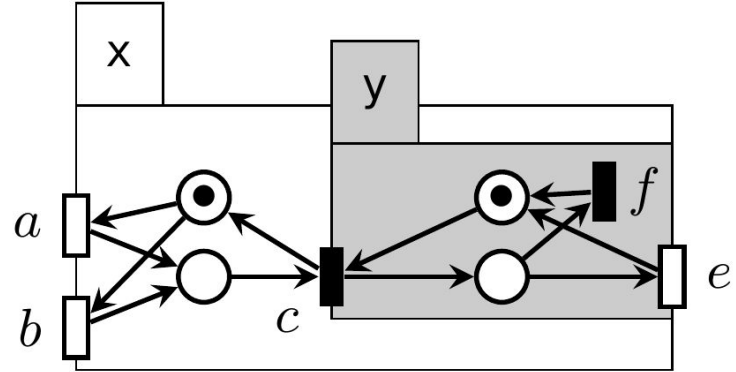
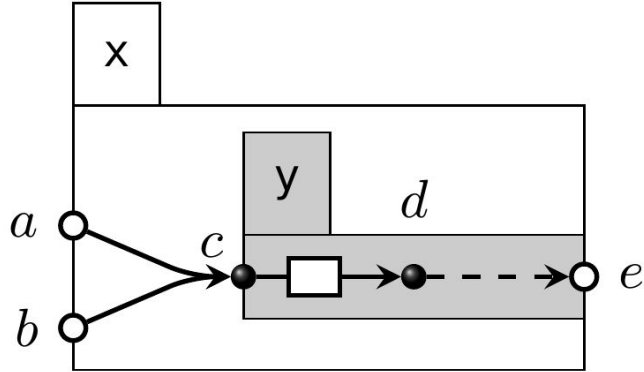
$\partial \langle \text{gateOpen} \rangle \text{true}$

Online tools <http://194.117.30.117>

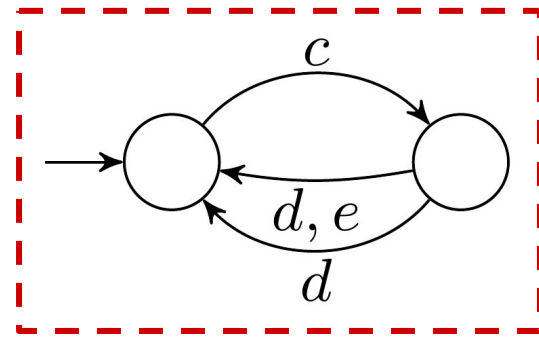
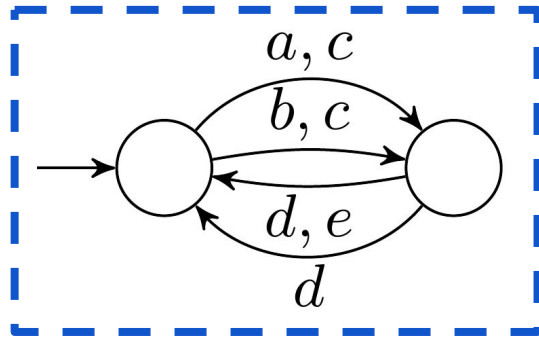
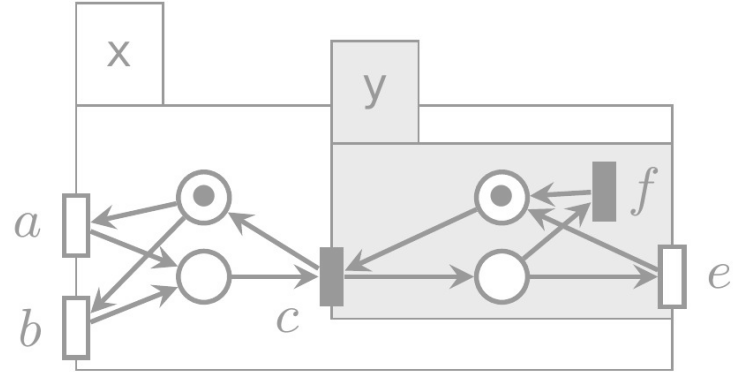
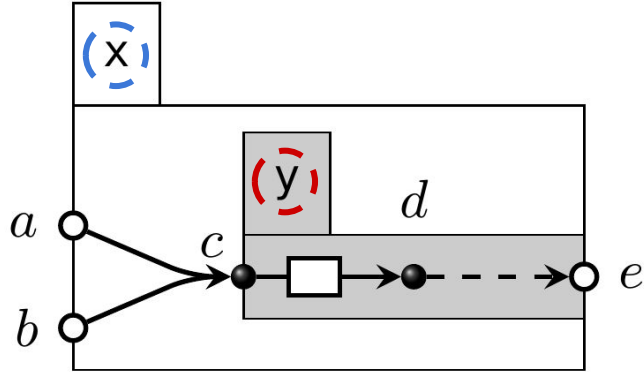
```
Input
1 switcher {
2   [hide] xor = ...,
3   [hide] alternator = ...,
4   [hide] gateOpen = ...,
5   [hide] gateClosed = ...,
```



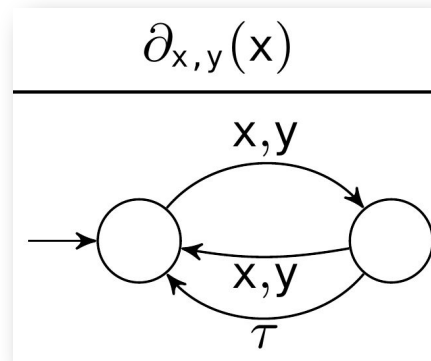
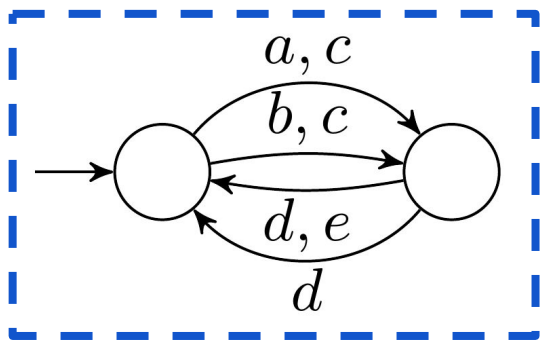
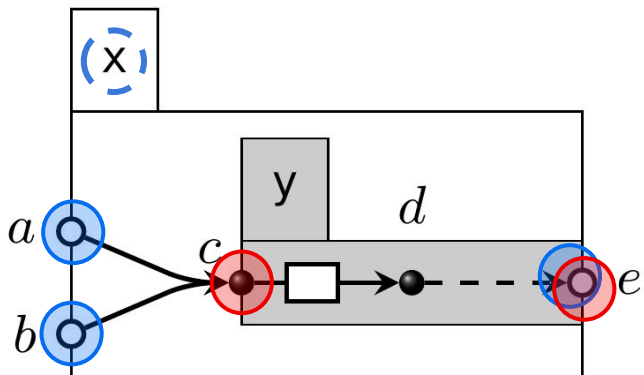
Hierarchical connectors



Hierarchical connectors

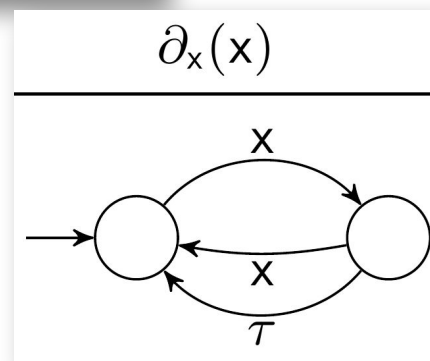


Container Abstraction

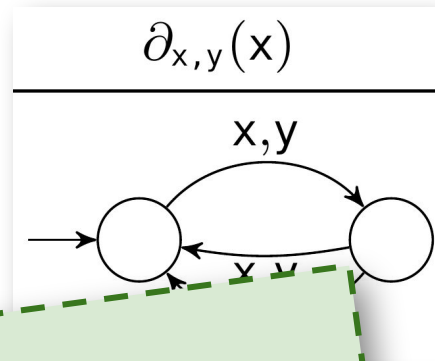
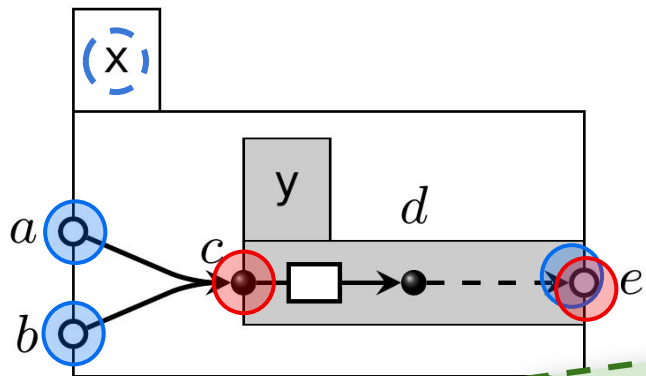


- $a \rightarrow \{x\}$
- $b \rightarrow \{x\}$
- $c \rightarrow \{y\}$
- $d \rightarrow \{\}$
- $e \rightarrow \{x, y\}$

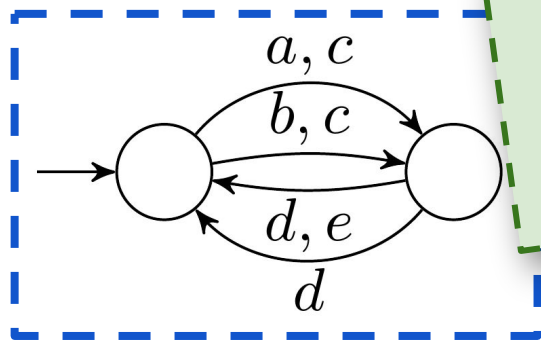
- $a \rightarrow \{x\}$
- $b \rightarrow \{x\}$
- $c \rightarrow \{\}$
- $d \rightarrow \{\}$
- $e \rightarrow \{x\}$



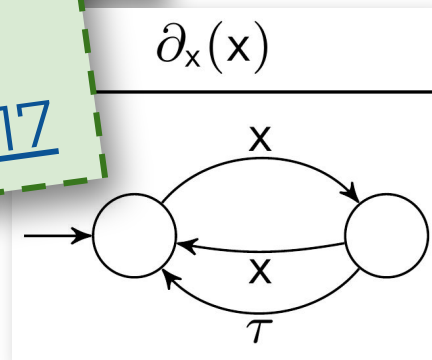
Container Abstraction



- $a \rightarrow \{x\}$
- $b \rightarrow \{x\}$
- $c \rightarrow \{y\}$
- $d \rightarrow \{\}$
- $e \rightarrow \{x, y\}$



Demo
<http://194.117.30.117>



- $c \rightarrow \{\}$
- $d \rightarrow \{\}$
- $e \rightarrow \{x\}$

Logic for Containers

$\psi := \text{true} \mid \text{false} \mid \langle \phi \rangle \psi \mid [\phi] \psi \mid @_c \psi \mid \partial \psi$ (state formula)

$\phi := \varphi \mid \phi^* \mid \phi + \phi \mid \phi . \phi$ (regular formula)

$\varphi := c \mid \tau \mid \text{all} \mid \text{none} \mid \bar{\varphi} \mid \varphi + \varphi \mid \varphi \& \varphi$ (action formula)

Based on



Hennessy-Milner with
regular modalities

Logic for Containers

Enter "c"

Go to parent

$\psi := \text{true} \mid \text{false} \mid \langle \phi \rangle \psi \mid [\phi] \psi \mid @_c \psi \mid \partial \psi$ (state formula)

$\phi := \varphi \mid \phi^* \mid \phi + \phi \mid \phi . \phi$ (regular formula)

$\varphi := c \mid \tau \mid \text{all} \mid \text{none} \mid \bar{\varphi} \mid \varphi + \varphi \mid \varphi \& \varphi$ (action formula)

Based on

M^CR^L2
analysing system behaviour

Hennessy-Milner with
regular modalities

Logic for Containers

$\psi := \text{true} \mid \text{false} \mid \langle \phi \rangle \psi \mid [\phi] \psi \mid @_c \psi \mid \partial \psi$ (state formula)
 $\phi := \varphi \mid \phi^* \mid \phi + \phi \mid \phi . \phi$ (regular formula)
 $\varphi := c \mid \tau \mid \text{all} \mid \text{none} \mid \bar{\varphi} \mid \varphi + \varphi \mid \varphi \& \varphi$ (action formula)

```
<all* . gate0open>  
  @gate0open <alternator* >  
  ∂ <gate0open> true
```

- At some point,
- gateOpen can interact twice
 - Without the alternator interacting

gateOpen and gateClosed
cannot interact in the same step

```
[all* . gate0open & gateClosed] false
```

Logic for Containers

$\psi := \text{true} \mid \text{false} \mid \langle \phi \rangle \psi \mid [\phi] \psi \mid @_c \psi \mid \partial \psi$

(state formula)

$\phi := \varphi \mid \phi^* \mid \phi + \phi \mid \phi \mid \dots$

(regular formula)

$\varphi := c \mid \tau \mid \text{all} \mid \dots$

(action formula)

Demo

<http://194.117.30.117>

$\langle \text{all}^* . \text{gateOpen} \rangle$

$@_{\text{gateOpen}} \langle \text{alternator}^* \rangle$

$\partial \langle \text{gateOpen} \rangle \text{true}$

at some point,

- `gateOpen` can interact twice
- Without the `alternator` interacting

$[\text{all}^* . \text{gateOpen} \ \& \ \text{gateClosed}] \text{false}$

`gateOpen` and `gateClosed`
cannot interact in the same step

Gained insights



Fine control over “**hiding**” is helpful:

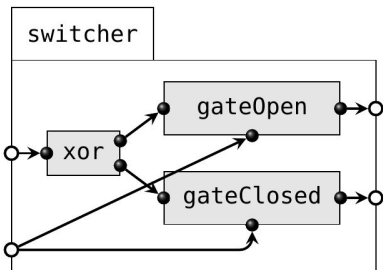
- For more **complex** connectors
- To reason about the **internals**
- To improve **performance** of model checking

What is a “ **τ** ” (tau)?

- *(there is room for improvements)*
- **τ** of `gateOpen`?
- Weak bisimilarity down to `gateOpen`, `gateClosed`

Wrap up

Hierarchical connectors



Container abstraction

Logic over containers

$\langle \text{all}^* . \text{gateOpen} \rangle$

$\text{@}_{\text{gateOpen}} \langle \overline{\text{alternator}}^* \rangle$

$\partial \langle \text{gateOpen} \rangle \text{true}$

Hiding mCRL2 generated details

Thank
you

Online tools

<http://194.117.30.117>

Still getting better...

```
Input
```

```
1 switcher {
2   [hide] xor = ...,
3   [hide] alternator = ...,
4   [hide] gateOpen = ...,
5   [hide] gateClosed = ...,
```

